

## CRACK MITIGATION IN POST-TENSIONED MEMBERS<sup>1</sup>

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### Q.1 MITIGATION OF RESTRAINT CRACKS

Post-tensioned members should be free to shorten, in order for the design-intended beneficial effects of post-tensioning to materialize. The background and computation of shortening of a post-tensioned member is discussed in the Technical Note (TN458). This Technical Note describes the practical steps that post-tensioning design engineers use in the United States both to allow for the shortening of post-tensioned members in their designs and to minimize the effects of restraint cracks.

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There are various detailing options for construction that can reduce the potential of crack formation. The selection of the proper detail depends, among other factors, on the amount of the anticipated shortening. Crack mitigation design has developed from the practice of design engineers over the years, and the observation of satisfactory performance of the post-tensioned floors where the details were used. The procedure is strictly empirical – that is to say, it is not derived from the principles of mechanics of solids.

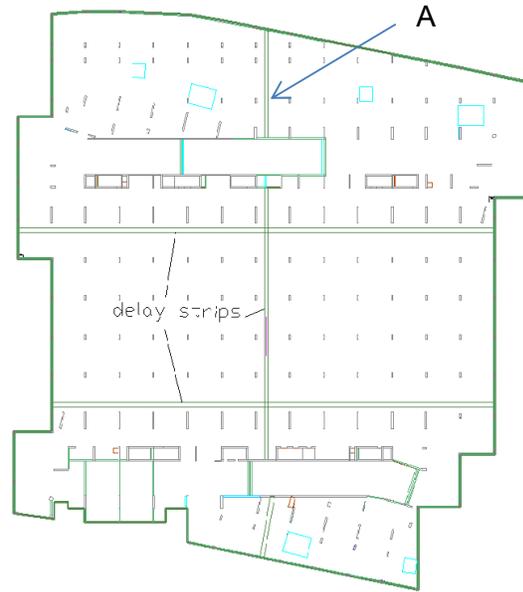
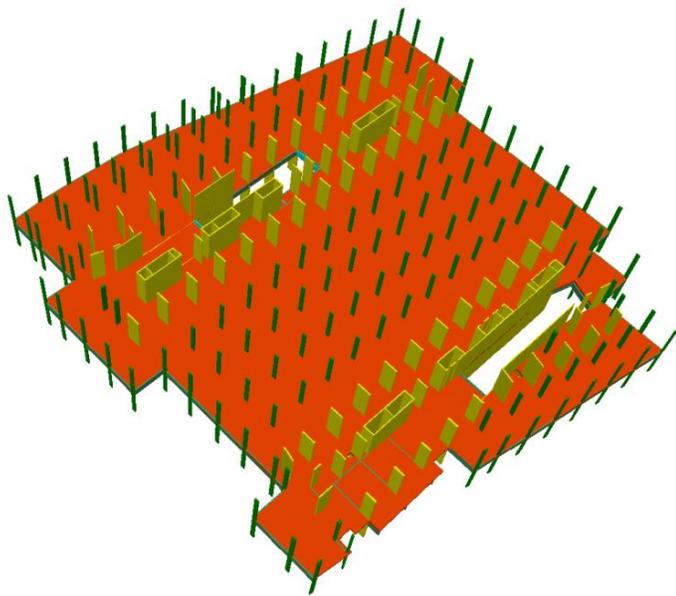
### **Q.1.1 Assumptions and Overview**

The principal assumptions for crack mitigation design of post-tensioned floors are:

- ❖ The shortening of a post-tensioned member is a time-dependent phenomenon. Under typical conditions, it will be at least two years before a post-tensioned member can be considered to have undergone its design-significant shortening. In typical construction, it is not practical for a post-tensioned member to be released from its supports long enough for the member to fully undergo its anticipated shortening. Where support restraints are significant, it is acceptable to allow occasional cracks.
- ❖ An acceptable limit (0.25 in.; 6 mm) to restraint shortening is established. The limit is the amount of computed movement of any point on a slab or beam that can be prevented from taking place because of restraint from the supports. In other words, if the computed long-term movement of any point on a post-tensioned member relative to its support does not exceed 0.25 in. (6 mm), the performance of the member with respect to shortening is deemed acceptable.
- ❖ For design purposes, the supporting walls are assumed not to shorten horizontally in the plane of the wall, but are free to bend normal to their plane
- ❖ Once a slab is tied to a wall, it is assumed that the slab's shortening parallel to the wall is fully restrained.

It is re-iterated that the above assumptions, as well as the methods of calculation and detailing that will be discussed, are empirical.

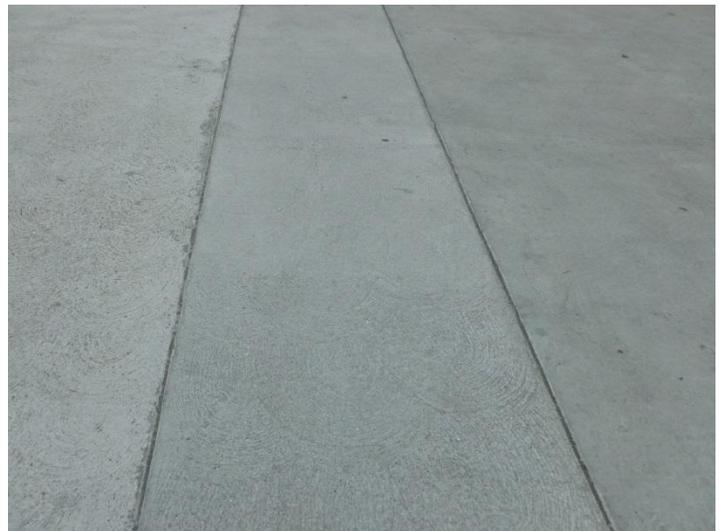
Consider the following example to illustrate the point. Figure Q.1.1-1a shows a post-tensioned floor slab of a podium construction that stretches over two levels of parking to serve two high rise towers one at each end. Recognizing the restraint of the towers and the perimeter walls to the free shortening of the post-tensioned slab between them, delay strips as marked on part (b) of the figure were provided. Delay strips – discussed in detail in Section Q.1.3.3.A – are gaps about 3 ft (1 m) wide that are left open between two segments of a post-tensioned slab, while the rest of the slab is cast. The objective of a delay strip is to allow the member on each side of it to undergo a certain amount of shortening, before the gap is filled to establish the continuity of the two segments on each side. Figure Q.1.1-2 shows an example of a delay strip in construction and after closure.



(a) Podium slab with towers on each side (P740)

(b) Identification of delay strips on slab (P741)

FIGURE Q.1.1-1 Post-Tensioned Slab with Delay Strips to Mitigate Cracking



(a) Delay strip in preparation using grouted tendons (P746)

(b) Delay strip closed and completed (P757)

FIGURE Q.1.1-2 Example of a Delay Strips before and after Closure

The question commonly facing a design engineer is “How long does the delay strip have to be left open ?” An open delay strip often hinders the progress of construction; contractors typically want to close the delay strip gaps as soon as possible.

As an example of how to determine this timing, consider delay strip ‘A’ in part (b) of the figure. Using the shortening calculations outlined in TN458 (Section P), it is determined that the total long-term shortening at this point will be 0.84 in. (21 mm); the shortening of each segment will thus be 0.42 in. (11 mm). This is more than the 0.25 in. (6 mm) that is

deemed acceptable. The delay strip must remain open until all but 0.25 in. of the shortening on either side of the strip has occurred. The following explains the calculation:

Total shortening on either side of the delay strip = 0.42 in. (11 mm)

Restrained shortening to be allowed = 0.25 in. (6 mm)

Shortening to take place, before closing the delay strip =  $0.42 - 0.25 = 0.17$  in. (4 mm)

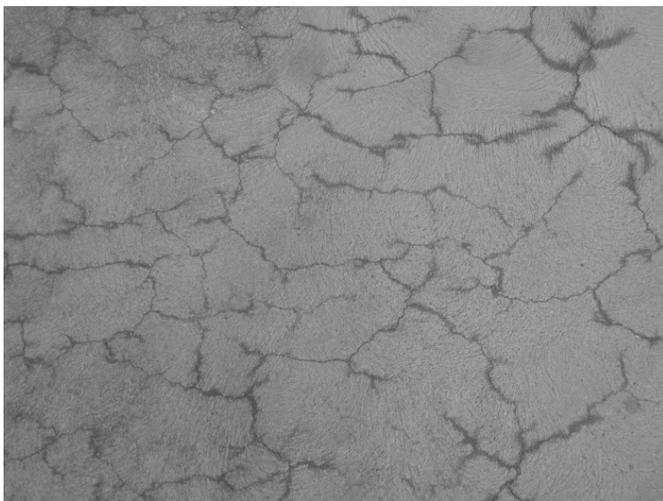
Ratio of unrestrained shortening to total shortening =  $0.17/0.42 = 0.41 = 41\%$

The delay strip has to remain open until 41% of the anticipated long-term shortening of the slab segments has taken place. Referring to Fig. P.2.7-1 of TN458, this corresponds to about 25 days, at which time approximately 41% of the computed shortening will take place. Thus, the delay strip should remain open for 25 days.

### Q.1.2 Characteristics of Restraint Cracks

Cracking is initiated when the stress in the concrete exceeds the concrete's tensile strength. Once initiated, the propagation and extent of cracking depends on the cause, as well as the detailing of the reinforcement at the crack location. For post-tensioned floor systems, three distinct crack types can be identified. These are: (i) plastic shrinkage cracks - shallow, closely-spaced irregular surface cracks caused by the shrinkage of improperly cured concrete (Fig. Q.1.2-1a); (ii) restraint cracks from the resistance of the supports to free shortening of the member; and finally (iii) strength cracks that occur when the applied moment exceeds the cracking moment of a section.

There are typically fewer restraint cracks than the other two types, particularly when unbonded tendons are used. The restraint cracks are generally wider, spaced farther apart and extend deeper into the slab than the other two types of cracks. In many cases, restraint cracks extend through the entire depth of a slab (Fig. Q.1.2-1 and 2).



(a) Shallow plastic shrinkage cracks (P753)



(b) Restraint crack, long and few in number (P751)

FIGURE Q.1.2-1 Plastic Shrinkage and Restraint Cracks

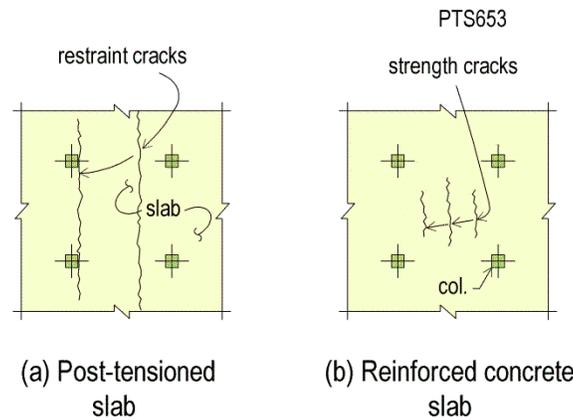


FIGURE Q.1.2-2 Plan of Reflected Ceiling; Cracking in Post-Tensioned and Conventionally Reinforced Slabs

In conventionally-reinforced concrete slabs, the spacing between the cracks is on the order of slab thickness, whereas in post-tensioned slabs the spacing is usually on the order of the length or width of the panel. In most cases, there is only one crack per panel in a post-tensioned slab. If there is more than one crack, the cracks are typically spaced at least one-quarter span apart. Restraint cracks in post-tensioned slabs typically do not occur at the locations of maximum moments, such as midspan or face of supports. They usually occur at axially weak locations like construction joints, delay strips, and where there are fewer reinforcing bars, such as at the end of the top bars over the supports.

Figure Q.1.2-3 shows two examples of typical restraint cracks in podium slabs constructed with unbonded tendons. In each case, the slab is the first elevated floor above the foundation. The long cracks shown extend through the entire depth of the slab. A significant portion of the post-tensioning in the longer direction has been diverted to the walls on the longer sides leading to a total loss of precompression in the left-right direction between the two long cracks (part b of the figure).

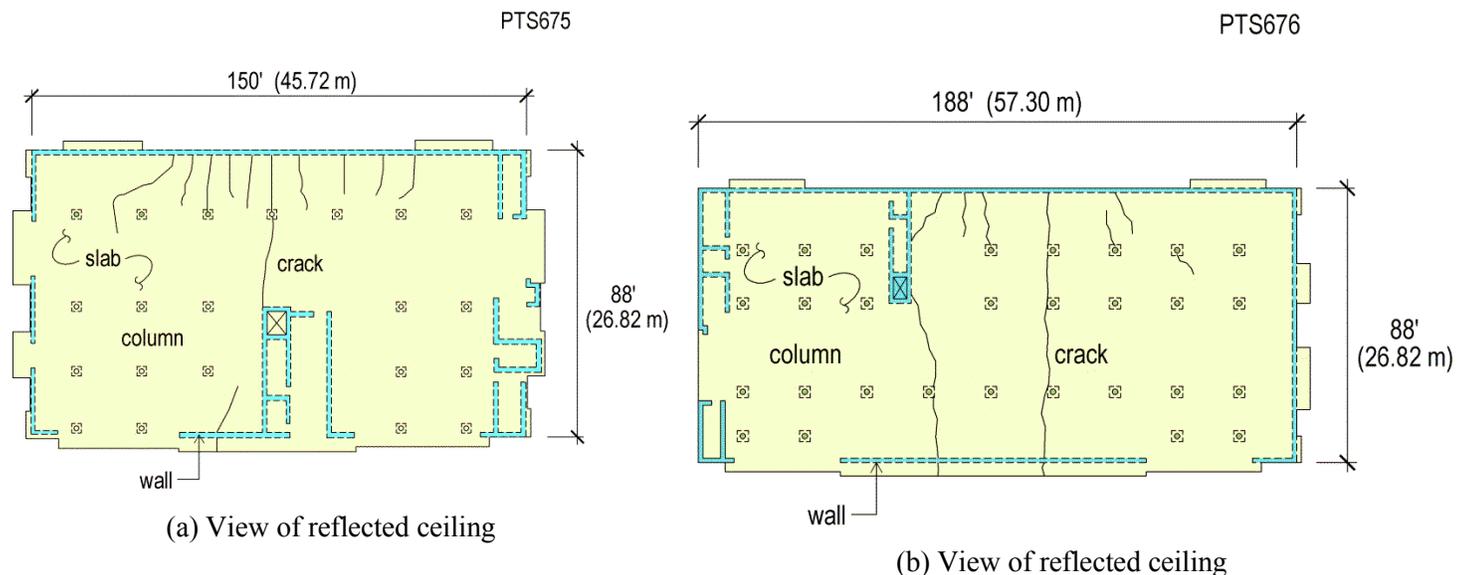


FIGURE Q.1.2-3 Plan of Reflected Ceiling; Restraint Cracks in Post-Tensioned Slab (Village Serramonte, CA)

Cracks due to local concentration of stresses at discontinuities (Fig. Q.1.2-4) in slab geometry can be reduced in width and number by addition of trim bars, but are difficult to fully eliminate, if the discontinuity is a cold joint between two

segments of a post-tensioned slab. Figure Q.1.2-5 is view of a discontinuity in a post-tensioned ground-supported slab. The addition of a large number of trim bars at the corners reduced the extent of the cracking, but did not fully eliminate it. Obviously, the slab has to crack before the trim bars can be effectively mobilized to control the width and extent of cracking. The same condition would apply to suspended slabs.

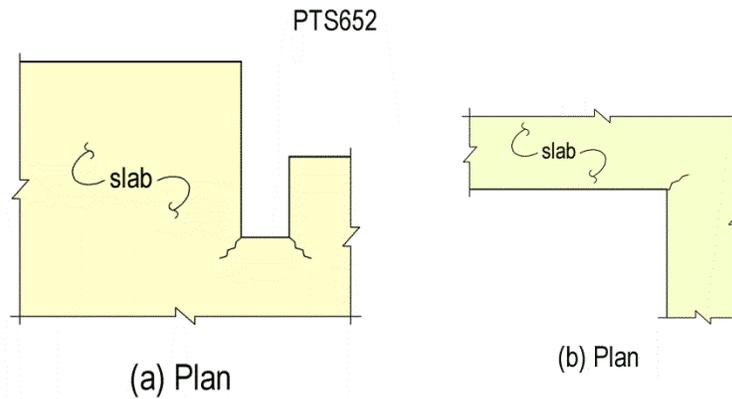


FIGURE Q.1.2-4 Cracking from Stress Concentration at Discontinuities (PTS652)



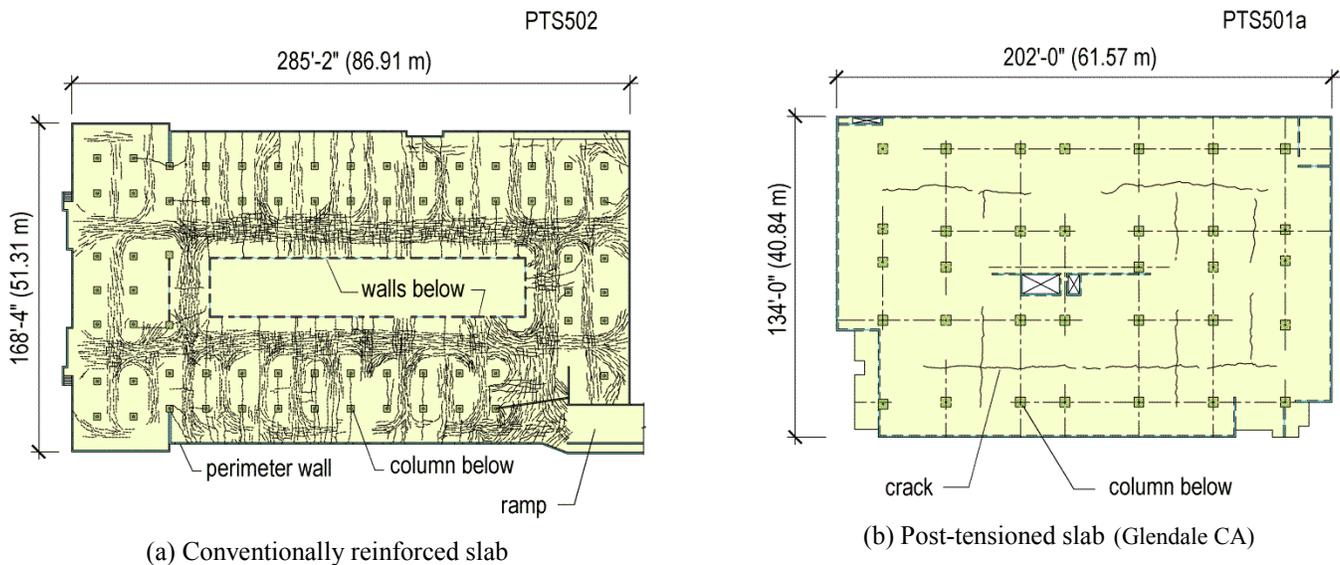
(a) Trip bars at construction joint (P758)



(b) Crack formation at construction joint (P759)

Q.1.2-5 Crack Formation at Discontinuities (Belly Rast Logistics Center; Moscow)

Cracks formed in a post-tensioned slab because of insufficient strength will be different from those caused by support restraint. They will also be different from those formed in a conventionally reinforced slab because of insufficient strength. As illustrated in Fig. Q.1.2-6, cracks due to shortfall of strength in post-tensioned slabs will be fewer in number than the corresponding conventionally reinforced slabs; will form at the locations of maximum demand in bending; and will not extend through the depth of the slab. In addition, strength cracks in post-tensioned members are often accompanied by noticeable deflections – a condition that is generally absent where cracking is due to restraint of supports.



Q.1.2-6 Plan of Reflected Ceiling; Crack Formation at Slab Soffit due to Shortfall in Strength

### Q.1.3 Crack Mitigation Options

The options available for crack mitigation can be categorized as follows:

- 1 – Favorable layout
- 2 – Structural separation
- 3 – Delay (closure) strips; joints; favorable pour sequence
- 5 – Permanent released connections
- 6 – Other released connections
- 7 – Detailing

It is emphasized, as will be discussed in Section Q.4.2, that these crack mitigation schemes are only necessary for the lower levels of a multi-story post-tensioned building. Crack mitigation may be necessary for the first, and possibly second and third levels above the foundation.

#### Q.1.3.1 Favorable Layout

Ideally the building can be designed with recognition of the shortening that will occur in the post-tensioned members and the supports will be located so as to minimize the restraint. But, while a desirable option, this is seldom possible. Fig. Q.1.3.1-1 shows support layouts that are favorable for crack mitigation and those that provide significant restraint to slab shortening,

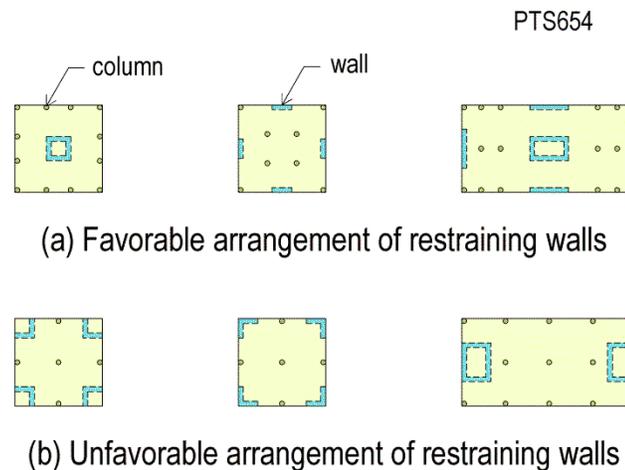


FIGURE Q.1.3.1-1 Examples of Favorable and Unfavorable Arrangements of Shear Walls for Mitigation of Restraint Cracks at Lower Levels of High Rise Buildings (P754) (PTS654)

### Q.1.3.2 Structural Separation

In some cases, it may be necessary to divide very large slabs into segments using permanent, structural separations. The following guidelines are suggested [Aalami, et al 1988].

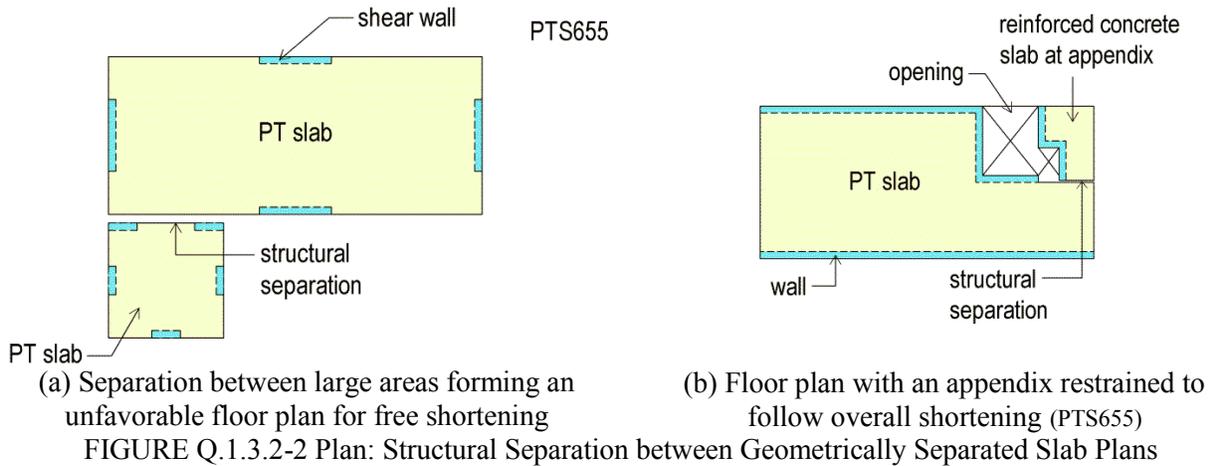
- ❖ Unless special provisions are made, limit the length of contiguous post-tensioned slabs to 375 ft (114 m). For slabs longer than 375 ft (115 m), provide a structural separation to reduce the potential for restraint cracks;
- ❖ For slabs longer than 250 ft (76 m), but not exceeding 375 ft (114 m), provide a central delay strip (closure pour); and
- ❖ For slabs or slab regions shorter than 250 ft (76 m), design the slab for the anticipated long-term shortening.

Figure Q.1.3.2-1 is an example of a structural separation (a physical gap separating two slab regions) for a long slab. Slabs with an irregular geometry are particularly vulnerable to cracking when restrained by supports. Figure Q.1.3.2-2a shows a small slab area appended to a larger rectangular shaped region. The structural separation shown in the figure between the two post-tensioned slab regions is designed to reduce cracking.

Structural separations are similar to expansion joints designed for temperature changes or separations designed to minimize damage from seismic events. The primary difference is that restraint separations are not required once the bulk of the slab shortening takes place (typically a period of several months). Thus restraint separations do not have to be designed to remain open and functional throughout the life of the structure. Also, restraint separations do not have to be continued through the entire height of the building; typically, two to three levels above the foundation will suffice. Seismic and temperature separations, on the other hand, should extend through the entire height of the building.



FIGURE Q.1.3.2-1 Plan; Structural Separation in a Long Post-Tensioned Floor Slab (P760)



**Q.1.3.3 Delay (closure) strips; joints; Favorable pour sequence**

The following describes the features of each of the crack mitigation schemes listed. An example demonstrates the application of each scheme.

**A. Delay Strips:** also referred to as closure or pour strips are temporary separations of approximately 36 in. (1 m) between two regions of slab which are constructed and post-tensioned separately. The width of the gap is to accommodate the length of the jacks that are generally used to stress the live end of the tendons that terminate on each face of the strip. Where tendons need not be stressed from the opening of the gap, the width of the delay strip can be much shorter. In this case, the gap will be wide enough to provide structural continuity between the overlapping reinforcement that extends from each side into the gap.

Cast regions on either side of the delay strip are allowed to shorten independently. Once the anticipated shortening has taken place, the gap between the two regions will be cast. Non-shrink concrete is preferred in filling the gap. The overlapping reinforcement that extends from the concrete slab into each side into the delay strip provides the structural continuity of the slab over the strip once the floor is placed in service. Figures Q.1.3.2A-1 and 2 show construction views of the several delay strips.



(a) Delay strip after concrete on one side is (P762)



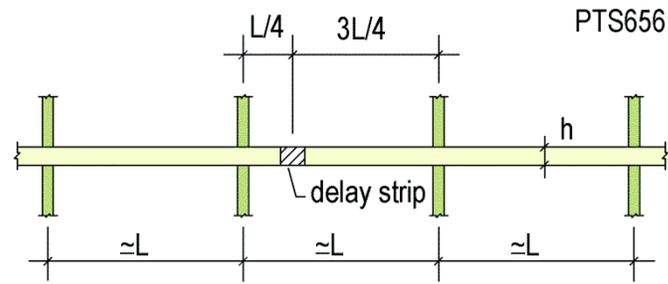
(b) Delay strip after concrete on both sides has been cast (P764)

FIGURE Q.1.3.2A-1 Delay Strips in Construction

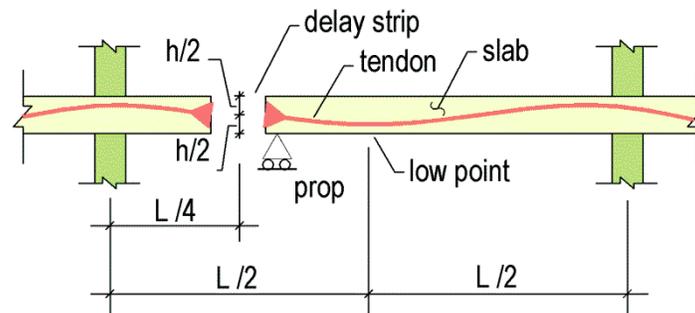


FIGURE Q.1.3.2A-2 Delay Strips in Podium Slab Joining a High Rise to Mitigate Crack Formation (P813)

If the support layout is such that the panels are all of approximately equal size, pour strips are typically located at the quarter span of a panel, because this is where the moment is the smallest (Fig. Q3.3.3A-2). The tendons are anchored at the centroid of the slab on each face of the strip. The tendon profile within the segments on either side of the gap should be as close as possible to the profile of the typical spans. Fig. Q3.3.3A-3 shows a computer model of the tendon arrangement at a delay strip. The short quarter-span overhang does not have to be supported, but the tip of the three-quarter span segment should be propped until the strip is cast and cured. Depending on the amount of post-tensioning, the short overhang will tend to rise, while the propped segment will tend to deflect downwards. In theory, there will be a lack of alignment between the two sides of the gap but in most slabs, the lack of alignment will be within construction tolerances.



(a) Elevation ; approx. equal spans



(b) Delay strip at quarter span

FIGURE Q3.3.3A-2 Suggested Delay Strip Location of Layout with Equal Spans (PTS656)

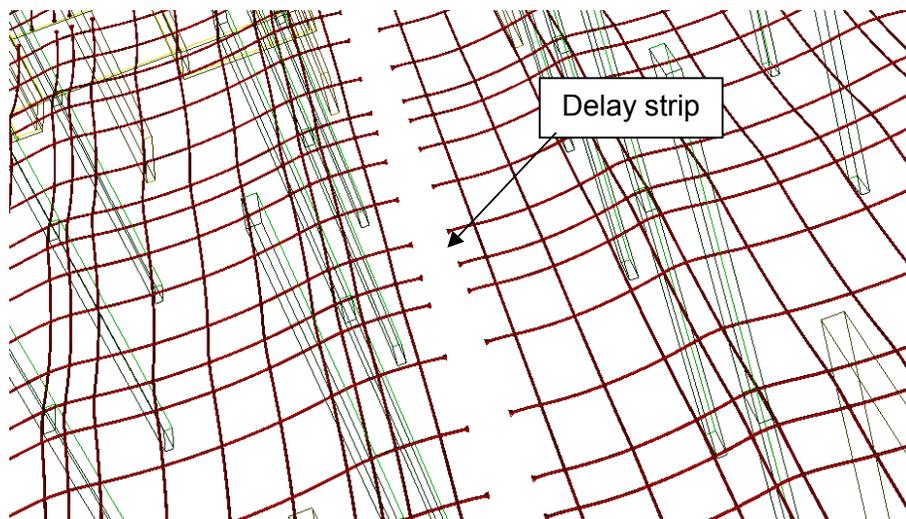
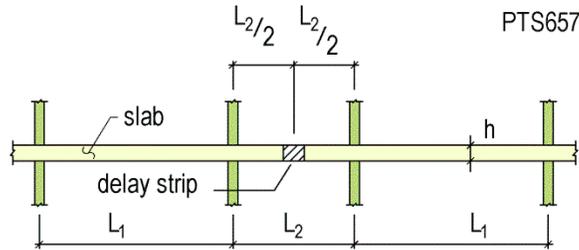


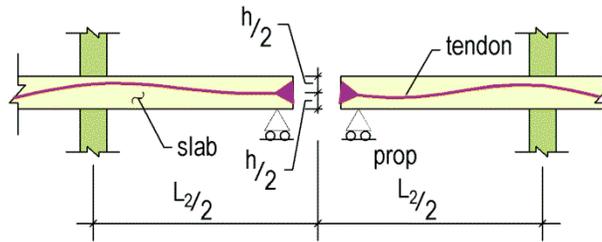
FIGURE Q3.3.3A-3 Example of a Tendon Layout with Delay Strip at Quarter Span, Showing the Overhang and Long-Span Tendon Profile (P764)

When the support layout results in different span lengths, the closure strip should be positioned in the middle of a short span, if possible (Q3.3.3A-4). The tendons from each side will again be anchored at the mid-depth of the slab; both slab edges should be propped until the gap is cast and cured.

Figure (Q3.3.2A-5) is an example of a delay strip located at mid-span. If the objective of the delay strip is to allow shortening of the slab and reduce cracking, it is generally not necessary to continue the delay strip through all levels of a multi-story building. Two to three levels will typically be adequate. If the objective is to provide access for stressing tendons, the delay strip will be required on all levels where such access is required.



(a) Elevation  $L_2 \ll L_1$



(b) Delay strip at mid span

FIGURE Q3.3.3A-4 Suggested Delay Strip Location of and Tendon Layout for Panels with Unequal Spans



FIGURE Q3.3.3A-5 Example of Delay Strip Positioned in Middle of a Span

Strictly speaking, the reinforcement of a delay strip falls in the realm of “phased construction”, where the design recognizes that the structure is constructed and subjected to load in more than one configuration – in this case selfweight and live load. There is commercially-available software<sup>3</sup> that handles the phased construction aspect of the delay strip, including allowance for the shortening that takes place while the gap is open. However, for common building construction, design engineers typically model the tendons as terminating at the delay strip (Fig. Q3.3.3A-3); design the member with the delay strip closed; determine the demand actions (moments, shears) across the gap; and design for them using conventional reinforcement. Fig. Q3.3.2A-6 shows the generic detail used for a delay strip in a post-tensioned slab with unbonded tendons.

Figure Q3.3.2A-7 shows a delay strip between a perimeter wall and a slab post-tensioned with bonded tendons. The delay strip runs parallel to the wall temporarily separating the floor slab from its support.

<sup>3</sup> ADAPT-ABI [www.ADAPTsoft.com](http://www.ADAPTsoft.com)

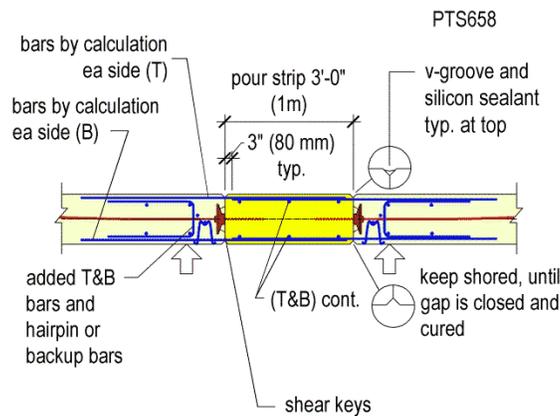


FIGURE Q3.3.3A-6 Typical Detail of a Delay Strip for Unbonded Tendon Construction (PTS658)



FIGURE Q3.3.3A-7 Delay Strip next to a Perimeter Wall Designed to Allow Stressing (P770)

**B. Joints:** Construction joints are separations that break an otherwise contiguous concrete slab into two concrete placements. One side of the joint is cast and allowed to cure before the adjoining part is placed. Once both sides are cast, the slab is intended to respond as a continuous member in resisting the applied loads. A construction joint (shown in Fig. Q3.3.3B-1a) differs from a cold joint in that (i) it is an intentional joint as that divides a large slab area into manageable pour sizes as opposed to the location at which a concrete batch is finished and (ii) there may be a delay of three to seven days between the first and second pour. The unrestrained joint allows the segment that is cast first to undergo a portion of its shortening before it is locked to the remainder of the structure.

Unlike delay strips, where the tendons terminate at the face of the strip gap, the post-tensioning tendons are continuous across a construction joint. To reduce the loss in prestress due to friction, long tendons are often stressed at the construction joint (part b of the figure).

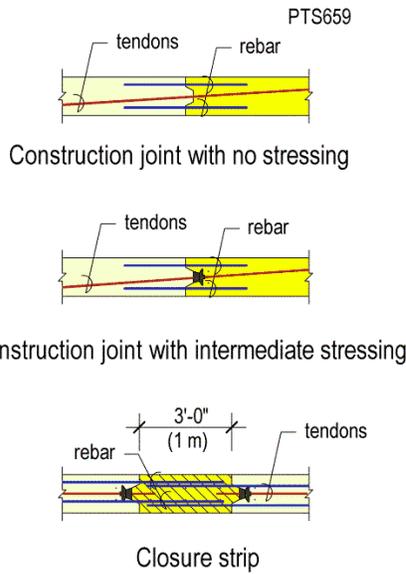


FIGURE Q3.3.3B-1 Several Options of Allowance for Temporary Shortening (PTS659)

Figure Q3.3.3B-2 is a schematic of construction joints with and one without intermediate stressing. Figure Q3.3.3B-3 shows a construction joint with intermediate stressing, where tendons from the cast side have already been stressed.



(a) Construction joint without intermediate stressing. (P659)      (b) Construction joint with intermediate stressing (P810)

FIGURE Q3.3.3B-2 Construction Joints with and without Intermediate Stressing. Recessed Shear Keys Enhances the Shear Transfer Across the Joint.

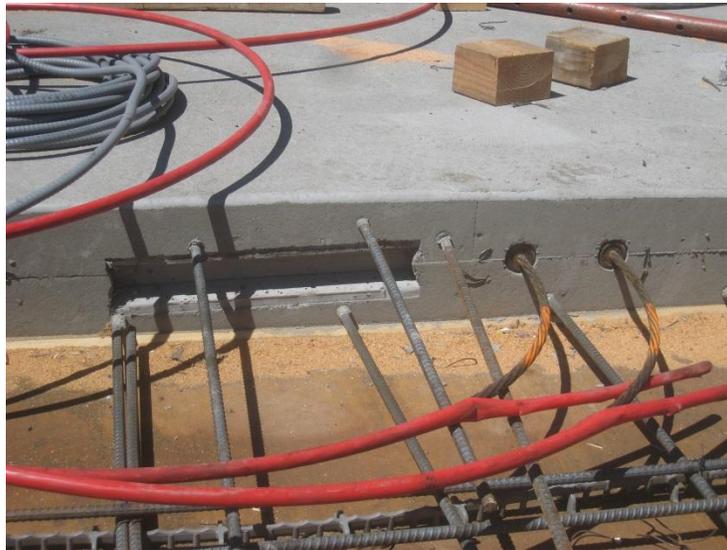
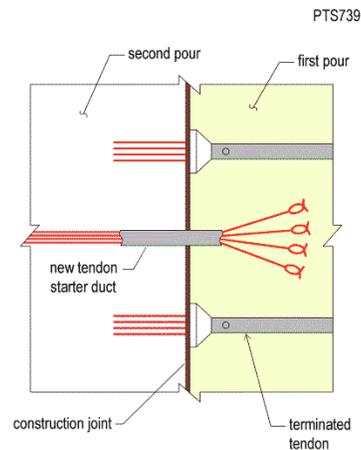


FIGURE Q3.3.3B-3 Construction Joint with Intermediate Stressing Showing the Shear Keys and Stressed Tendons (P812)

Not all bonded post-tensioning systems include the hardware required to allow stressing at a construction joint. The alternative is either to terminate the tendon at the face of the joint or use two partial-length tendons and overlap the dead (fixed) ends at the construction joint.



(a) Overlapping tendons at a construction joint with intermediate stressing (P765)



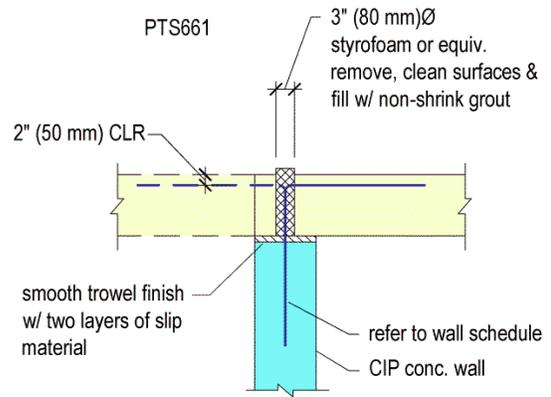
(b) Construction joint with intermediate stressing using couplers

Q3.3.3B-3 Construction Joints with Intermediate Stressing

**C. Temporary Released Connections:** Temporary release connections allow a post-tensioned member to shorten for a limited period of time by allowing it to freely slide over its support before it is locked to the support for full force transfer. The most common temporary release connections are between walls and slabs. Figure Q.1.3.3C-1 shows two examples of temporary releases. In each case, the wall is separated from the slab through a slip material. In part (a), the relatively flexible corrugate tube is initially filled with a compressible material. Once the slab is cast and has undergone its design-intended shortening, the compressible material is removed and the tube is filled with high strength grout to establish the means of horizontal force transfer between the wall and slab. In part (b) the dowels extending from the lower wall into the slab are initially encased in a non-rigid material such as Styrofoam. The non-rigid material is removed and replaced with non-shrink grout to fix the connection.



(a) Dowels extend into slab (P766)



(b) Structural detailing of the release (PTS661a)

FIGURE Q.1.3.3C-1 Temporary Release between Wall and Slab. The Fill in the Corrugated Tube in part (a) is Replaced with Grout

Figure Q.1.3.3C-2 is another example of a temporary release. The wall is topped with slip material and dowels from the lower wall will connect to the wall above. The tubes will be grouted once the required amount of shortening has occurred.

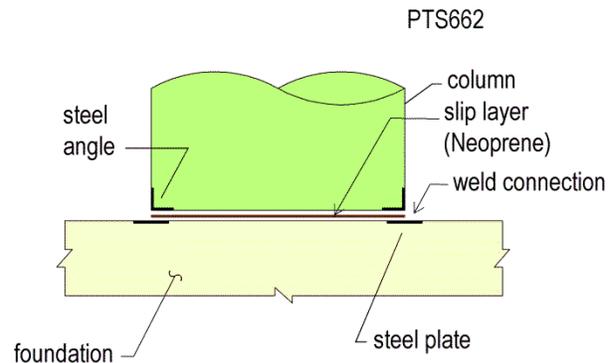


FIGURE Q.1.3.3C-2 Example of a Slab Release; Walls from below Tie to the Walls above (P810).

A column/slab release can also be provided at the base of a column. In the case of the Moscone Exhibition Hall in San Francisco, the heavy construction long-span roof of the hall required strong columns that at the base would have restricted the shortening of the roof under post-tensioning. The bases of the columns were separated from the foundation by elastomeric (Neoprene) pads. After the roof had undergone sufficient shortening, steel angles embedded in the columns were welded to plates embedded in the foundation, thus providing the necessary fixity for the column-foundation connection (Fig. Q.1.3.3C-3).



(a) Column base on slip pad (P767)



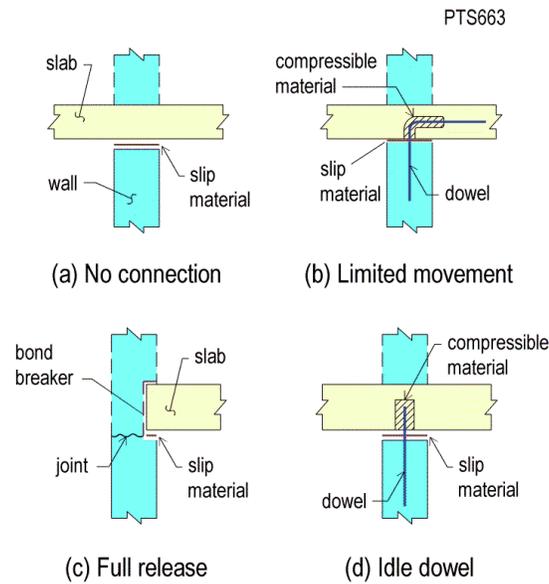
(b) Schematic of temporary base connection (PTS662)

FIGURE Q.1.3.3C-3 Example of a Temporary Column Base Foundation Release (San Francisco)

**D. Favorable Pour Sequence.** Large slabs are typically broken down into pours of around 2000 sf (approx. 200 m<sup>2</sup>). This size can be handled by a typical construction crew and corresponds to the amount of formwork that small to medium size contractors stock. For improved crack mitigation, the pours should be done in a checkerboard sequence, to allow as much free shortening of each slab segment as possible. This, however, is not possible in all cases and will probably not be how the contractor would prefer to sequence the pours.

**Q.1.3.4 Permanent Release Connections:** Permanent release connections are used when there is no structural need for force transfer between the slab and its support in the direction of the release. A permanent release allows unimpeded movement between the slab and its support at the release. Permanent release connections come in different styles. A permanent wall/slab release can be used when only vertical forces need to be transferred from the slab to the wall; the forces in other directions, such as forces from wind or earthquake, will be designed to be transferred to the supports at other connections.

Figure Q.1.3.4-1 shows the schematics of several wall/slab connections. Examples are shown in Fig. Q.1.3.4-2. The usefulness of the dowel shown in Fig. Q.1.3.4-1(d) is questionable. Its purpose is to restrain horizontal displacement of the slab relative to its support in a catastrophic event, such as a major earthquake. But it is unlikely that a bar of that size without positive anchorage in the slab would provide much resistance to a catastrophic event that could move the slab support off the wall. The detail shown in Fig. Q.1.3.4-1(b) allows movement within the limits anticipated by the slab shortening, but will provide resistance in a catastrophic event.



Q.1.3.4-1 Schematics of Several Wall/Slab Release Options



(a) Permanent release for horizontal movement (P768)



(b) Permanent wall slab-band release (P769)

Q.1.3.4A-2 Construction Examples of Wall-Slab Permanent Releases

**Q.1.3.5 Other Release Connections**

Unusual slab geometries, slabs with limited access for stressing, or slabs where even a small amount of restraint will lead to objectionable cracking may require specifically-tailored release connections. The following illustrates the common occurrence of a post-tensioned floor between two below-grade walls where there is no access for stressing at the slab edge. The plan (Fig. Q.1.3.5-1) shows stressing blockouts alternating between the two sides of the slab. The stressing blockouts are spaced so that there is about 8 ft (2.50 m) of wall support between each opening. The combination of the support from the wall and the reinforcement in the slab eliminate the need for shoring while the stressing blockout is open. Details of the stressing blockout are shown in Fig. Q.1.3.5-2.

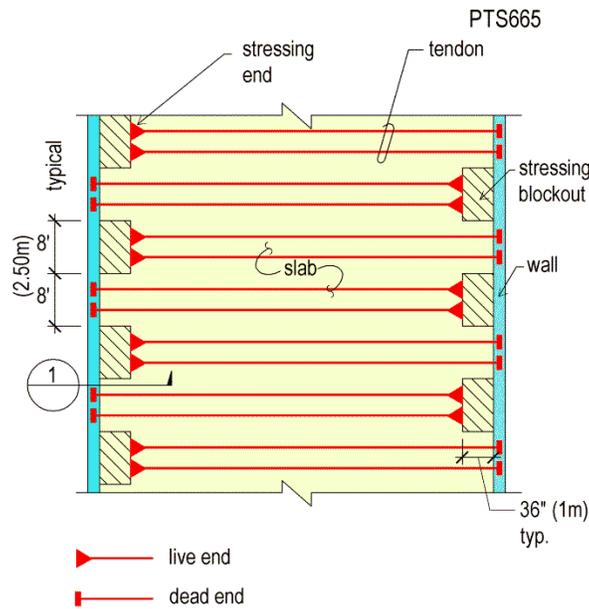


FIGURE Q.1.3.5-1 Plan; Slab between two Excavated and Shored Walls

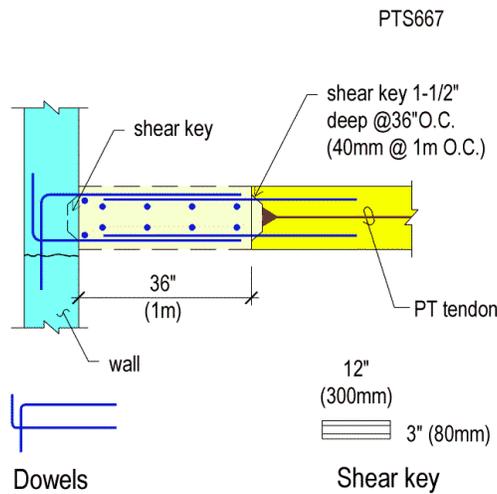


FIGURE Q.1.3.5-2 Detail of Stressing Blockout at Wall

There are many variations of slab/wall and other types of releases, each developed to suit the specific application.

**Q.1.3.6 Detailing**

Judicial arrangement and/or addition of post-tensioning tendons and non-prestressed reinforcement can be used to minimize the formation of restraint cracks.

**A. Favorable Arrangement of Tendons:** In certain conditions it is practical to arrange tendons, or to terminate them such as to either avoid significant drop in precompression, or to provide added precompression to combat stress concentration from discontinuities in the geometry of construction. The following are examples.

Figure Q.1.3.6A-1b shows an alternative arrangement of tendons around an opening to the regular straight layout. The alternative arrangement results in adding precompression to the perimeter of the opening, as opposed to causing tension by pulling apart the sides of the opening in part (a).

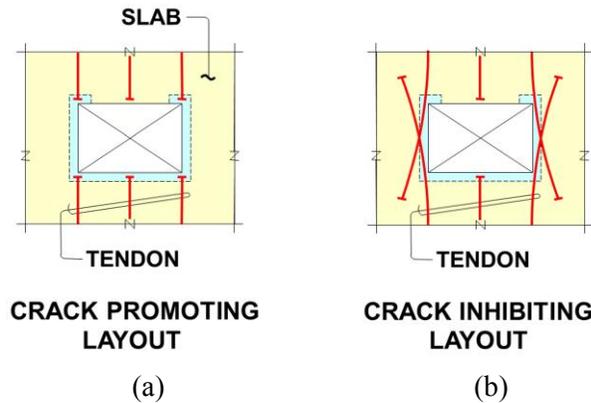


FIGURE Q.1.3.6A-1 Alternative Arrangement of Tendons around Openings (P789)

Where there are interior walls that can provide significant restraint to the free shortening of a post-tensioned slab and thus absorb some of the precompression from the tendons, overlapping of tendons as shown in the plan of Fig. Q.1.3.6-2 can be beneficial. It is emphasized that the restraint of the walls shown in the figure is of concern primarily at the lowest levels of a multistory frame. At upper levels the restraint provided by the walls is greatly reduced, and the measure shown in the figure will not be necessary (Aalami, 2014).

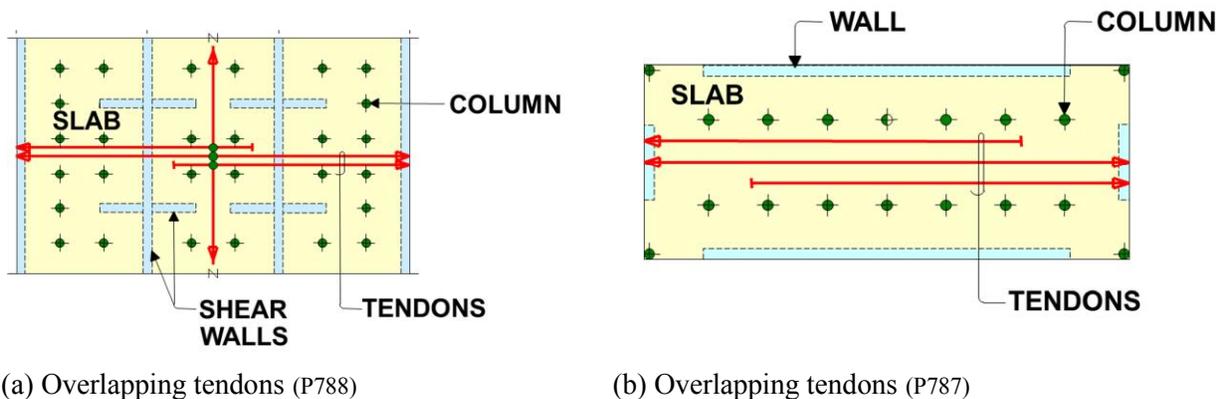
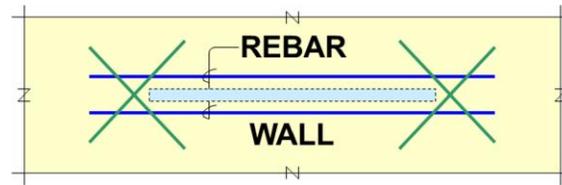
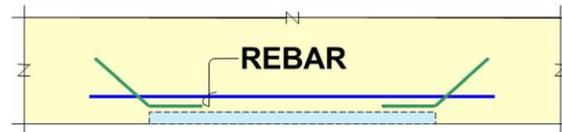


FIGURE Q.1.3.6-A2 Overlapping Tendons at the Interior Region of Slab to overcome Loss of Precompression from the Walls

**B. Detailing of Non-Prestressed Reinforcement:** Non-prestressed reinforcement can be used to reduce the width of cracks that result from restraint of the supports and to increase the crack in number. A single wide and long restraint crack can be reduced to a multiple short and narrow cracks to make them visually more acceptable. Two typical examples to control restraint cracks adjacent to the walls at lower levels of post-tensioned floor constructions are shown in Fig. Q.1.3.6B-1 and 2.



(a) INTERIOR SHEAR WALL



(b) EXTERIOR SHEAR WALL

FIGURE Q.1.3.6B-1 Crack Control Detailing Bars adjacent to Walls at Lower Levels of Post-Tensioned Floors (P786)

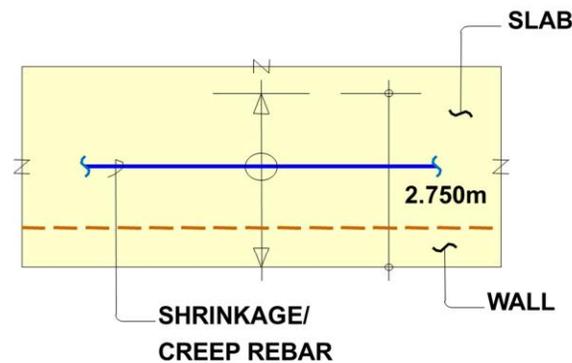


FIGURE Q.1.3.6B-2 Crack Control Detailing Bars adjacent to Continuous Walls at Lower Levels of Post-Tensioned Floors (P785)

Unlike trim bars stated above for restraint of supports to free shortening of post-tensioned floors, trim bars to control cracking at locations of stress concentration, such as opening must be used at all levels of a post-tensioned building, where a discontinuity occurs. A typical example is trim bars around openings as shown in Fig. Q.1.3.6B-3.

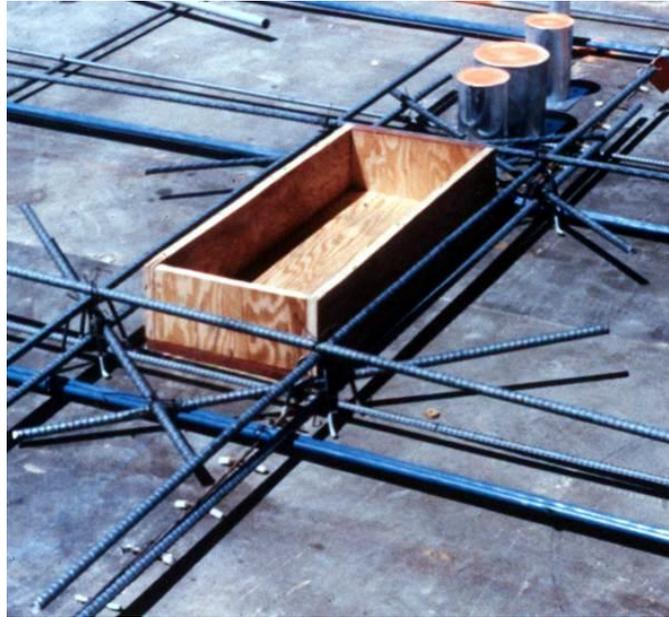


FIGURE Q.1.3.6B-3 Trim Bars around Openings (P784)

#### Q.4 CRACK MITIGATION EXAMPLES

In this Section, the practical aspects of design for crack mitigation design will be illustrated through two examples. The first example is a structure with a high degree of restraint requiring extensive measures to allow for the shortening of its post-tensioned floor slab. The measures and details used in this example are commonly used for similar construction in the US. The second example is the shortening calculation and crack mitigation design for a multi-story building in California.

The first step in crack mitigation is to determine the anticipated long-term shortening of the post-tensioned member. The shortening calculation is outlined in Section Q.2. In the absence of detailed computations or for preliminary designs, it is acceptable to assume 0.75 in. of shortening for every 100 ft of slab length (10 mm shortening for every 15 m of slab length). This is the value that is generally assumed for the floor slabs of residential and commercial buildings constructed in the US.

##### Q.4.1 Podium Slab on Perimeter Walls

A common type of residential construction in parts of California where land is expensive is to build one or two levels of parking below, or at, grade. The parking levels are constructed of post-tensioned concrete, with the slab over the top level of parking acting as a podium to support up to five levels of light framing superstructure. The light framing, in most cases, is wood construction. The floor slabs of the parking levels are usually flat slabs supported on interior columns and perimeter walls. Figure Q.4.1-1 is a typical example, where a concrete frame consisting of one level of subterranean parking and a retail level at grade, support four levels of wood frame apartment housing.



FIGURE Q.4.1-1 Apartment Building with Post-Tensioned Underground Parking and Retail at Street Level (Redwood City, CA; P791)

The plan geometry of the podium slab is as shown in Fig. Q.4.1-2. The interior columns are not shown because they do not impact the crack mitigation design.

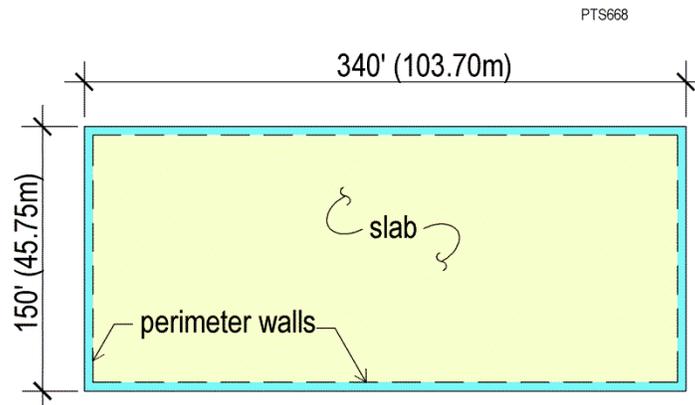


FIGURE Q.4.1-2 Plan; Overall Geometry of the Post-Tensioned Slab

The structural and construction requirements of the design are:

- ❖ Each of the long walls needs a minimum of 150 ft (45.75 m) of shear wall. This requires full connection and transfer of horizontal forces in addition to gravity between the wall and the slab.
- ❖ Each of the short walls needs a minimum of 100 ft (30.5 m) of shear walls.
- ❖ If a delay strip is provided, it may not be kept open more than a total of 20 days. This is to avoid interruption in the construction schedule.

**A. Consult Crack Mitigation Guidelines:** Referring to Section Q.1.1, since the length of the slab exceeds 250 ft (76 m) but is less than the length requiring a structural separation, design the slab with a central delay strip. This reduces the length that must be designed for shortening before the delay strip is closed to 170 ft (51.85 m).

Using the assumption that the long-term shortening of the slab will be 0.75 in. per 100 ft of length (10 mm per 15 m), the segments on either side of the delay strip must be designed for the following shortening:

$$\text{Total shortening at each end of each slab segment} = 170 \times 0.75 / (100 \times 2) = 0.64 \text{ in. (16 mm)} > 0.25 \text{ in. (6 mm)}$$

The anticipated long-term shortening is thus larger than what can be accommodated without crack mitigation measures.

**B. Wall/Slab Full Connection Length to be Cast with Slab:** At this step, we determine the maximum length of the slab/wall connection that can be cast at the same time as the slab and detailed for full shear transfer between the slab and the wall.

The maximum length of the slab ( $b$ ) that can be detailed and cast with full shear transfer to the wall, while satisfying the requirement that shortening relative to the wall at any point not exceed 0.25 in. (6 mm) is:

$$b = [(2 \times 0.25) / 0.75] \times 100 = 67 \text{ ft (20.44 m)}$$

The length  $b$  is shown in Fig. Q.4.1B-1.

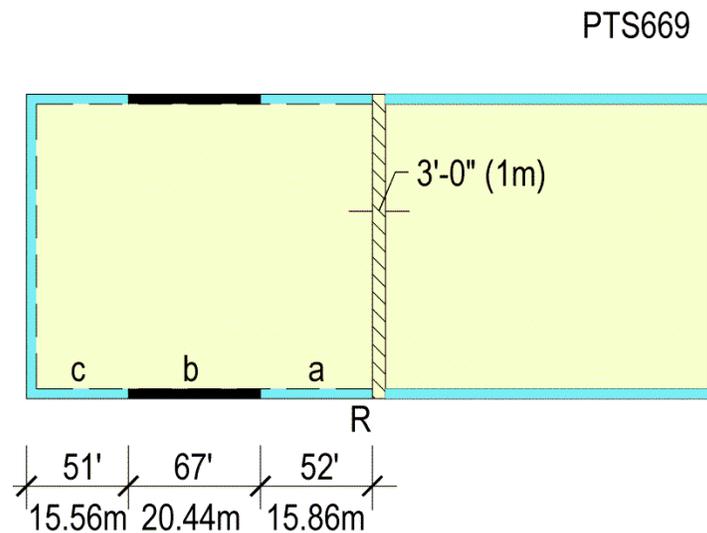


FIGURE Q.4.1B-1 Plan – Post-Tensioned Slab Partially Designed for Crack Mitigation (PTS669)

**C. Determine the Position of Full Connection Length:** The length ( $a$ ) shown in Fig. Q.4.1B-1 is determined so as to allow the end at the delay strip (Point  $R$ ) to have undergone all but 0.25 in. (6 mm) of its anticipated long-term shortening when the delay strip is cast on day 20. Once section ( $b$ ) of the wall shown in Fig. Q.4.1B-1 is locked to the slab, it is assumed, for crack mitigation design, that the ends of the segment remain fixed in position. Hence, the entire shortening of the slab segment ( $a$ ) will have to take place from point  $R$  at the delay strip.

Refer to Fig. Q.2.7-1 (shortening with time) to estimate the fraction of the long-term shortening that will have taken place by day 20, since at day 20 segment  $a$  will be locked to the wall and the delay strip, and further shortening will be prevented. The value read from the graph for day 20 is 36%. To ensure that no more than 0.25 in. of shortening occurs after day 20, the maximum acceptable long-term shortening of segment ( $a$ ) is:

$$\text{Slab (a) total shortening} = 0.25 / (1 - 0.36) = 0.39 \text{ in. (10 mm)}$$

Using again the assumption of 0.75 in. per 100 ft (10 mm per 15 m), the distance ( $a$ ) is calculated as follows:

$$a = 100(0.39 / 0.75) = 52 \text{ ft (15.85 m)}^4$$

<sup>4</sup> The slight discrepancy is due to the soft conversion of 0.75" per 100' to 10 mm per 15 m

**D. Verify the Adequacy of Slab to Wall Full Connection:** The structural design requirements call for 150 ft (45.75 m) of shear wall connection between the slab and the wall in the long direction. The length ( $b = 67$  ft; 20.44 m) calculated for the initial connection must ultimately be increased to at least 75 ft (22.88 m) on each side of the delay strip to meet the connection requirements for shear force transfer between the wall and the slab. Figure Q.4.1D-1 shows the connection at slab section (a) as a “temporary release.” A temporary release is a connection that allows relative movement between the slab and its supporting wall until the movement is prevented by establishing full fixity. A possible detail for a temporary release is shown in Fig. Q.4.1D-2. In this detail, a relatively flexible plastic pipe is initially filled with a compressible material such as compacted newspaper. To fix the connection, after the slab is cast and the anticipated shortening taken place, the compressible material is removed and the pipe is filled with high-strength grout. The floor plan shows the entire length ( $a$ ) as detailed with this temporary release. Once the delay strip at the center of the floor slab is cast, both ends of the strip ( $a$ ) will be prevented from shortening; in effect the entire length of strip ( $a$ ) will be fixed in position when the delay strip is cast and fixity between the slab segments on the two sides of the delay strip is established.

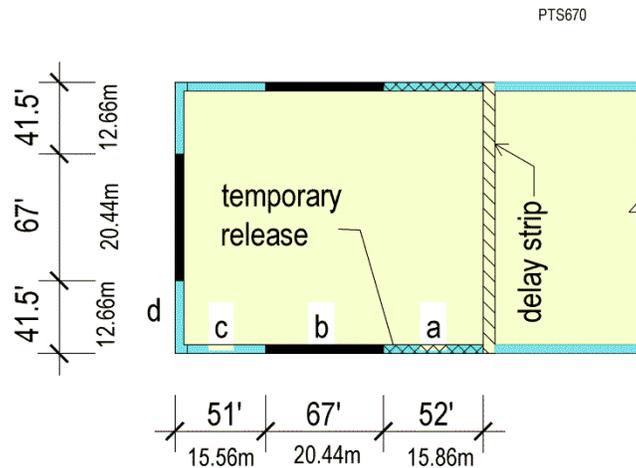
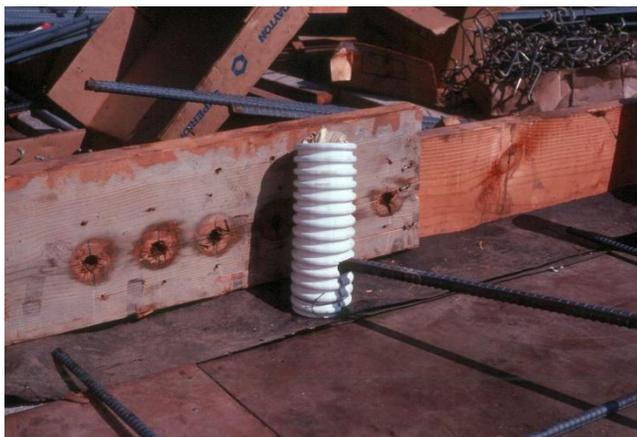
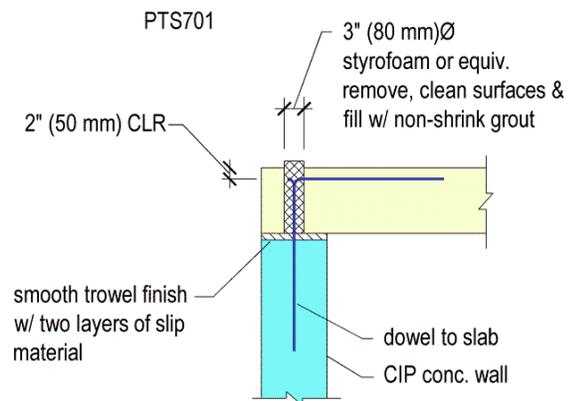


FIGURE Q.4.1D-1 Connection between Slab and wall



(a) Tube covers dowel (P773)



(b) Detail of temporary release

FIGURE Q.4.1D-2 Temporary Release Connection between Slab and Wall  
Top of wall is finished with two layers of slip material

**E. Detail the Remainder of Slab/Wall Supports:** Since section (c) of the slab is almost the same length as section (a), it is assumed that sufficient shortening will have taken place by day 20 that the slab section can be locked to the wall at that point. In practice, however, for improved crack mitigation, it is better to leave any connection that is not required by design to be fixed as a “permanent release.” The release at slab corners avoids the formation of cracks shown in Fig. Q.4.1E-1. As shown in Fig. Q.4.1E-2, a length of 10 ft (3 m) is often left as a permanent release at the corners. In this example, because of the long length of the slab, a length of 20 ft (6.1 m) is detailed as a permanent release. Figure Q.4.1E-3 is an example of a permanent release at a slab corner, where two sheet layers of manufactured woods are used to separate the slab from the wall and allow the slab to move with respect to the wall. The remainder of segment *c* is designated as a temporary release.

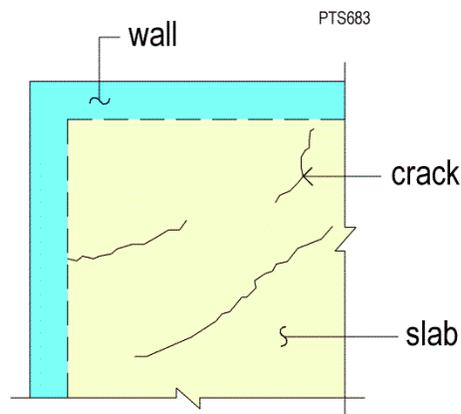


FIGURE Q.4.1E-1 Cracking at Restrained Corners of Post-Tensioned Floors

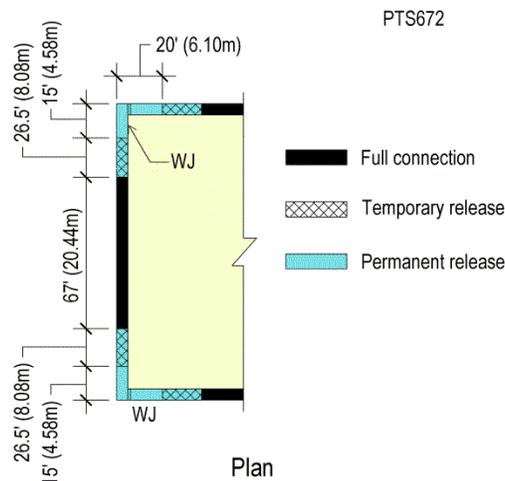
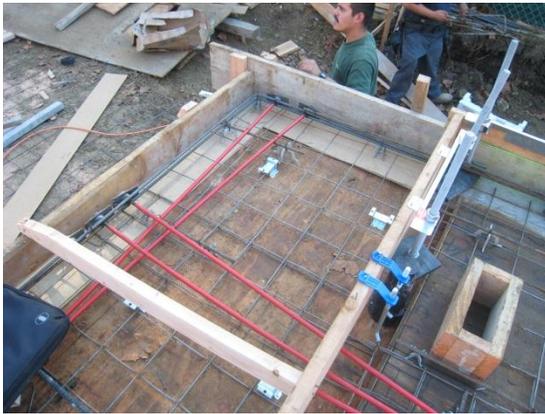


FIGURE Q.4.1E-2 Slab/Wall Connection Plan (PTS671)



(a) Permanent release at slab corner, showing two layers of slip sheet on top of wall (P809)



(b) Manufactures sheets used for slip join (P775)

Q.4.1E-3 Detail of Permanent Slab/Wall Release Showing the Installation of Slip Material as Slab Corner

**F. Design of the Short Wall Connection:** From the design for the long direction it was determined that 67 ft (20.44 m) of full connection between the wall and the slab can take place at the time the slab is cast. For the short wall, the balance of the required length for 100 ft (30.5 m) of full connection results in:

$$\text{Required full connection at each end} = (100 - 67)/2 = 16.5 \text{ ft (5.03 m)}$$

Thus, it will be necessary to provide a temporary release over a 16.5 ft (5.03 m) length of slab at each end of the full connection. The connection can be locked on day 20 when the delay strip is cast.

**G. Review of Detailing:** Recognizing that the procedure is highly empirical and derived from the practice of design engineers in the field, once the computations are completed, engineering judgment is exercised to conclude the design with practical construction details. When finalizing the details, attention is paid to irregularities in the geometry of the slab and its supports, including interior wall connections, such as commonly exist at elevators and stair wells.

The final detailing of the connections is shown in Fig. Q.4.1G-1, where a permanent release of 15 ft (4.58 m) is considered adequate for the short wall. Where a permanent release is intended, the top of the wall must be trowel finished to a smooth surface and then covered with a slip material. The slip material often used is two layers cut from sheets of  $\frac{1}{4}$ -in. (6 mm) manufactured wood<sup>5</sup>. The sheets are smooth on one face (Fig. Q.4.1E-3); the smooth sides are placed face to face, to allow free movement between the two sheets. The advantage of this material is that it is stiff enough to bridge over small irregularities, in case the top of the wall is not adequately smooth.

<sup>5</sup> Trade name "Masonite"

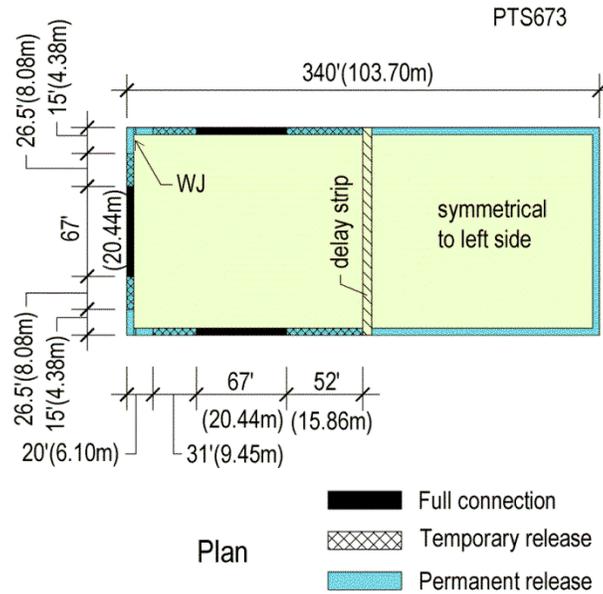


FIGURE Q.4.1G-1 Completed Design of the Crack Mitigation Scheme

Where practical the intersecting wall corners are provided with a wall joint (marked WJ on Fig. Q.4.1G-1) that has a gap of about  $\frac{3}{4}$  in. (20 mm). The wall joint is intended to provide the short wall greater freedom to bend out of its plane in following the shortening of the slab. Figure Q.4.1G-3 shows a wall joint along with a wall/slab joint provided with slip material. A view of the slip strips on top of the wall prior to casting the slab is shown in Fig. Q.4.1E-3.



(a) Wall joint as support corner (P778)



(b) Wall/slab connection with slip layers (P779)

FIGURE Q.4.1G-3 Wall Joint and Slab/Wall Connection with Slip Material (show picture before concrete is poured)

### Q.4.2 Example of a Multistory Building

Construction of post-tensioned multi-story buildings fall in the category of “phased construction,” also referred to as “Segmental Construction,” where the structural members are installed and placed in service one after the other. Further, during the construction, previously installed members will be subject to loads, stresses, and deformations that impact the response of the completed structure to its in-service design load. The “phased construction” analysis of concrete structures

with detailed consideration of long-term effects is well understood and coded in commercially available software<sup>6</sup>. However, for practical design of common residential and commercial buildings, empirical and approximate schemes can be used to account for the shortening of the floor slabs from post-tensioning and the restraint of the supports to the shortening.

These empirical methods have been validated by the satisfactory performance of buildings where they have been used. To a great extent, however, the successful application of these methods rests on the experience and the engineering judgment of the designer.

The factors causing shortening of a floor slab and the calculation of this shortening are detailed in Section Q.2. The assumptions and procedures to account and allow for the shortening are discussed in Sections Q2 and Q.1, followed by a numerical example for a single level structure. When dealing with multistory buildings, in addition to the assumption that 0.25 in. (6 mm) of shortening is acceptable, the following assumptions are made.

At the first elevated floor, the shear walls are assumed to be fixed to the foundation. At the upper levels of a multistory building, the shear walls are more elastic as they are less restrained by the foundation. The walls thus provide less restraint to slab shortening. Table Q.4.2-1 can be used to obtain an initial estimate of the shortening that can be accommodated by the upper levels of a multistory building. The table distinguishes between single walls and compound walls such as T-shaped, U-shaped, or core walls.

Using the table, at the 4<sup>th</sup> elevated level and above, single walls are assumed to provide no restraint to the shortening of the floor slab. Referring to the table again, at the third elevated level above the foundation, for a “core wall”, it is assumed that the long-term movement accommodated by the wall at the wall/slab connection is 3 mm (0.12 in.). If the “calculated” floor shortening at this level is 8 mm (0.31 in.), the amount of shortening that needs to be designed for is 5 mm (8 – 3 = 5 mm; 0.2 inch). Since the slab is assumed to be able to accommodate a larger amount of shortening, namely, 6 mm (0.25 in.), no crack mitigation measures will be necessary.

The values in Table Q.4.2-1 are for construction where each level of the wall is cast right after the slab below is cast. When core walls such as those for the elevator shafts are constructed several levels above the floors, lower values should be assumed for the amount of slab shortening that the walls can accommodate, as the walls will have undergone some amount of shrinkage before the slabs are cast. In addition, core walls are generally in the shape of C, U or a box. Compared to single walls, core walls provide a larger restraint to the horizontal movement that could accommodate slab shortening.

TABLE Q.4.2-1 The Amount of Shortening Accommodated by Walls that Support Post-Tensioned Floors (T189)

Level	Single walls	Core/ compound wall
1 <sup>st</sup> level	0	0
2 <sup>nd</sup> level	0.125 in. (3 mm)	0.06 in. (2 mm)
3 <sup>rd</sup> level	0.25 in. (6 mm)	0.12 in. (3 mm)
4 <sup>th</sup> level	No restraint	0.18 in. (5 mm)
5 <sup>th</sup> level	No restraint	0.25 in. (6 mm)
6 <sup>th</sup> level	No restraint	No restraint

<sup>6</sup> ADAPT-ABI [www.adaptsoft.com](http://www.adaptsoft.com)



**B. Long-Term Shortening of Typical Floor:** The design length of the floor slab is taken as 202.50 ft (61.76 m) plus one half of the length encompassed by the end walls.

Design length of the slab in the long direction =  $202.50 + 33 = 235.5$  ft, rounded to 235 ft (71.68 m)

In the short direction, the design length is 66.50 ft (20.28 m)

From the calculations detailed in Section H, the anticipated shortening of a typical level of the building in the long direction is estimated as 1.38 in. (35 mm)<sup>7</sup>.

Anticipated shortening at each end =  $1.38/2 = 0.69$  in.  $> 0.25$  in. (17.5 mm  $> 6$  mm),

Hence design for crack mitigation is required.

**C. Crack Mitigation for Typical Floor:** The construction schematic and schedule of construction for a typical 7-day cycle of upper level floors is shown in Fig. Q.4.2C-1 and listed in Table Q.4.2C-1. A typical floor level (*i*), as indicated in the figure will be locked to the remainder of construction at stage 6 of each cycle, when the additional shortening of the locked slab will be restrained.

Each slab is tied to the shear wall through its dowel connection with the wall above it (Fig. Q.4.2C-1). From the schedule of construction shown in figure and listed in the table, the time lapse between locking the movement of a freshly cast floor to the wall below it is five days. The construction detail shown in the figure allows the slab to shorten freely within this 5-day period.

In multi-story buildings such as the current project, as a floor slab shortens, it draws the walls that it is tied to with it. Based on the sequence and schedule of construction given above, the following observations are made:

- ❖ The movement of each cast slab is locked to the structure after five days through the slab connection with the wall above.
  - ❖ When a floor slab is locked to the walls above it, the slab and the wall above rest on the wall immediately below. The newly cast slab and the wall above will be subject to the long-term movement of the wall below to which they are locked. Following the schedule of construction, one arrives at the conclusion that on the day the current slab (level *i*) is locked to the remainder of the construction through its dowels to the wall above, the floor slab at the level below (level *i-1*) is 12 days old.
    - ❖ The newly cast slab will continue to shorten. The wall that supports this slab is tied to the slab of the level below that will also continue to shorten, albeit with a seven day ( $12-5 = 7$ ) time gap.
- ❖ The long-term anticipated differential shortening of a floor slab and the slab immediately above and below is the difference between the shortening that takes place between days 5 and 12. This is the shortening that will be resisted by the restraint of the shear walls at the ends of the building and is subject to design for crack mitigation.

From long-term shortening graph Q.2.7-1:

<sup>7</sup> In the absence of detailed calculation followed here, the estimated shortening would be  $235.5 \times 0.75 / 100 = 1.75$  in. (44 mm)

The fraction of the long-term shortening that has taken place by day 12 is 28 %

The fraction of the long-term shortening that taken place by day 7 is 16 %

The restraint of the end walls to the slab shortening thus corresponds to  $(28 - 16) = 12$  % of the calculated long-term shortening.

This amounts to  $0.12 \times 0.69 = 0.08$  in. (2 mm) < 0.25 in. (6 mm) OK

Since the shortening that will take place after the slab has been tied to the supports is less than 0.25 in. (6 mm), no crack mitigation measures are necessary for the typical upper levels of the building. The above conclusion is based on the premise of the empirical Table Q.4.2-1, from which the walls at the upper levels do not require to be designed for restraint of supports. The restraint design carried out was based on the differential shortening between adjacent levels.

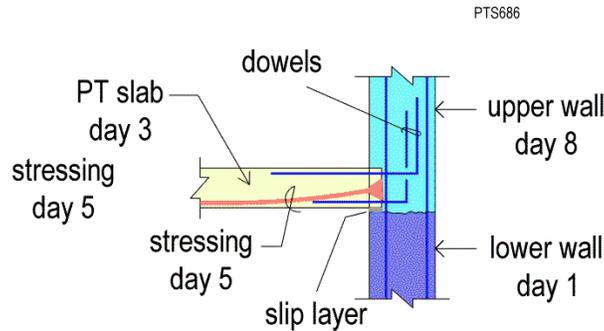


FIGURE Q.4.2C-1 Section; Slab-Wall Connection Detail; Construction Sequence and Schedule

TABLE Q.4.2C-1 Construction Schedule (T190)

Stage	Day	Operation
1	1	Cast wall for upper slab support
2	2	Finish forming of slab ( <i>i</i> ) above and place reinforcement
3	3	Cast slab ( <i>i</i> )
4	5	Stress tendons of slab ( <i>i</i> )
5	6,7	Form slab of level above ( <i>i</i> +1) and upper walls
6	8	Cast upper walls ( <i>i</i> +1)
7	9	Finish forming of slab ( <i>i</i> +1) above and place reinforcement
8	10	Cast slab ( <i>i</i> +1)
9	12	Stress tendons of slab ( <i>i</i> )
10	13,14	Form slab of level above ( <i>i</i> +2) and upper walls
11	15	Cast upper walls ( <i>i</i> +2)

**D. Crack Mitigation Design of the First Elevated Floor: D. Crack Mitigation Design of the First Elevated Floor:**

Referring to the estimate of the long-term shortening of the typical level, the anticipated shortening of the first floor will be the same — 1.38 in. (35 mm). From Table Q.4.2-1, it is assumed that the walls at the first elevated slab are completely rigid and will not accommodate any shortening. Because of the amount of anticipated shortening, it will be necessary to provide delay strips at both shear walls as well as at the center of the slab. This will allow the shrinkage to occur at both ends of each slab segment. The tendons in each slab segment will be short enough that they only have to be stressed at one end. The delay strip at the center should be wide enough to allow for stressing (Fig. Q.4.2D-1); the delay strips at the shear walls do not have to be designed for stressing (Fig. Q.4.2D-2). Contrary to what is shown in Fig. Q.4.2D-1a, the delay strip at the connection with the end wall can be narrower as shown in part (b) of the figure.

Total long-term shortening at each end of each slab segment =  $1.38/4 = 0.35$  in. (9 mm)

Since the slab is assumed to be able to accommodate 0.25 in. (6 mm) of shortening, the amount of shortening that must take place freely (before the delay strips are filled) is calculated as follows:

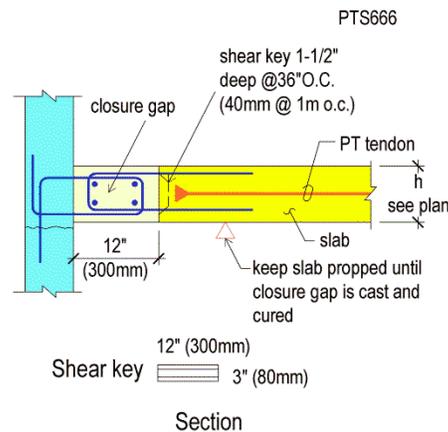
Shortening to take place =  $0.35 - 0.25 = 0.1$  in. (2.5 mm)

Fraction of total shortening to take place freely is:  $0.1/0.35 = 0.28 = 28\%$

Referring to Fig. Q.2.7-1, this corresponds to 40 days. Hence, at the first elevated level, the delay strips should be left open for 40 days.



(a) Detail of delay strip at connection to wall. There is a gap between the end face of the wall and slab (P792)



(b) Delay strip at wall with no stressing

FIGURE Q.4.2D-1 Delay Strip at Wall. (The gap at the face of the wall in part (a) can be narrower when tendons will not be stressed at the delay strip)

**E. Crack Mitigation of Second Elevated Floor:** The long-term shortening of the second elevated floor slab in the long direction will be the same as the typical level - 1.38 in. (35 mm). If the slab is divided into halves like the first elevated floor, the unrestrained shortening of each half will be:

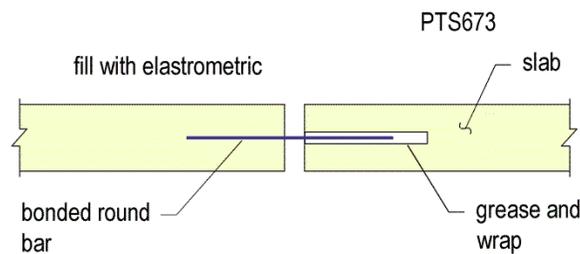
Total shortening at each end of each slab segment =  $1.38/4 = 0.35$  in.  $> 0.25$  in. (9 mm  $>$  6 mm)

From Table Q.4.2-1, the connection of the wall to the slab at this level is assumed to accommodate 0.125 in. (3 mm).

The balance of the shortening will be:  $0.35 - 0.125 = 0.225$  in.  $< 0.25$  in. (approx. 6 mm) OK

Since at the connection to the wall, the remainder of the computed shortening is less than 0.24 in. (6 mm), the same detail and stressing schedule as used for the typical level can be adopted. Note that at this level, the provision of a central slip joint at the middle of slab (Fig. Q.4.2.E-1) reduces the shortening that needs to be allowed at the wall/slab connection. Thus enabling the same detail as in typical levels to be used.

Details of the permanent release used at the center of the floor slab is shown in Fig. Q.4.2.E-1.



(a) Section: Permanent Release in Slab



(b) Permanent Slab Release  
Figure Q.4.2E-1

**F. Crack Mitigation of Third Elevated Floor:** The third elevated floor is detailed as a typical level.

**G. Comments on the Adopted Mitigation Scheme:** A section view of the structure with the crack mitigation detailing is shown in Fig. Q.4.2G-1. Recognizing that the methods used to design the crack mitigation scheme are highly empirical, engineering judgment must be used to adjust the design, taking into account both irregularities in the geometry of the slab and construction requirements.

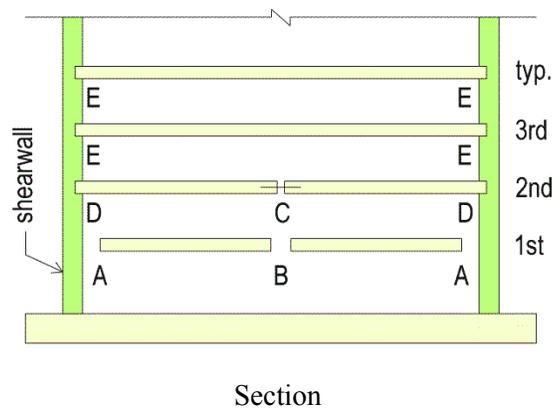


Figure Legend: A: Q.4.2D-2; B: Q.4.2D-1; C:Q.4.2E-1;D and E: Q.4.2C-1.

FIGURE Q.4.2G-1 Partial Section of Building

**H. Computation of Unrestrained Shortening of Typical Floor:** Using the procedure outlined in Section Q.2 of TN458, the unrestrained shortening of a typical level is calculated as follows:

Design Parameters

Concrete strength,  $f'_c = 6000$  psi (41 MPa)

Concrete strength at stressing,  $f'_{ci} = 3000$  psi (20.7 MPa)

Relative humidity,  $H = 70\%$

Slab thickness = 7 in (178 mm)

Seasonal change in temperature = 35  $F^\circ$  (19  $C^\circ$ )

$P/A$ , longitudinal direction = 125 psi (0.86 MPa)

$P/A$ , transverse direction = 150 psi (1.00 MPa)

Shortening Calculations:

❖ Elastic shortening strain,  $ES$ :

$$ES = (P/A) / E_{ci}$$

$$E_{ci} = 33 \times 150^{1.5} \sqrt{3000} = 3,320,560 \text{ psi (22,895 MPa)}$$

In SI units the calculation is :

$$E_{ci} = 0.043 \times 2400^{1.5} \sqrt{20.7} = 23,002 \text{ MPa}$$

Hence, the elastic shortening strain of the slab ES is:

$$\text{For longitudinal direction } ES = (125/3320560) = 38 \times 10^{-6}$$

$$\text{For transverse direction } ES = (150/3320560) = 45 \times 10^{-6}$$

❖ Shrinkage shortening strain, *SH*:

$$SH = SH_0 \times k_{RH} \times k_{v/s}$$

$SH_0$  = applicable base shrinkage strain = 510 micro-strains

Correction for relative humidity  $H = 70\%$ .

$$k_{RH} \text{ for } 70\% = 1.00$$

Correction for volume to surface ratio:

$$V/S = 0.5 \times 7 = 3.5 \text{ inch (0.5} \times 178 = 89 \text{ mm)}$$

The correction factor  $k_{v/s}$  is:

$$k_{v/s} = [1064 - 94 \times 3.5] / 923 = 0.80 \quad \text{US units (inch)}$$

$$k_{v/s} = [1064 - 3.7 \times 89] / 923 = 0.80 \quad \text{SI units (mm)}$$

Hence the long-term shrinkage strain is:

$$SH = 510 \times 10^{-6} \times 1.00 \times 0.80 = 408 \times 10^{-6}$$

❖ Creep shortening strain, *CR*:

$$CR_c = CR_0 \times K(PT) \times k_f \times k_{cRH} \times k_c$$

$CR_0$  = applicable base creep coefficient = 2.0

Correction for concrete strength  $k_f, f'_c = 6000 \text{ psi (41 MPa)}$

$$k_f = 1 / (0.67 + 6/9) = 0.75 \quad \text{(US units)}$$

$$k_f = 62 / (42 + 41) = 0.75 \quad \text{(SI units)}$$

Correction for relative humidity

$$k_{cRH} = (1.58 - H/120)$$

$$k_{cRH} = (1.58 - 70/120) = 1.00$$

Correction for volume to surface ratio:

$$V/S = 0.5 \times 7 = 3.5 \text{ inch (0.5} \times 178 = 89 \text{ mm)}$$

The correction factor  $k_c$  is:

$$k_c = \left[ \frac{1.80 + 1.77 e^{-0.54 \times 3.5}}{2.587} \right] = 0.80 \quad \text{US units}$$

$$k_c = \left[ \frac{1.80 + 1.77e^{-0.0213 \times 89}}{2.587} \right] = 0.80 \quad \text{SI units}$$

Having obtained the correction factors, the creep coefficient is given by:

$$CR_c = 2.0 \times 0.75 \times 1.00 \times 0.80 = 1.20$$

$$\text{For the longitudinal direction, the creep strain, } CR = CR_c \times ES = 1.20 \times 38 \times 10^{-6} = 46 \times 10^{-6}$$

$$\text{For the transverse direction, the creep strain } CR = CR_c \times ES = 1.20 \times 45 \times 10^{-6} = 54 \times 10^{-6}$$

❖ Strain due to seasonal change in temperature:

$$TEMP = T \times \alpha$$

$$TEMP = 35 \times 6.0 \times 10^{-6} = 210 \times 10^{-6}$$

❖ Total shortening strains, not accounting for seasonal change in temperature:

$$a = L ( ES + SH + CR + TEMP )$$

In the longitudinal direction:

$$S = (38 + 408 + 46 + 210) \times 10^{-6} = 702 \text{ micro-strains}$$

In the transverse direction:

$$S = (45 + 408 + 54 + 210) \times 10^{-6} = 717 \text{ micro-strains}$$

❖ Shortening,  $a$ , not including temperature effects :

In the longitudinal direction:

$$\text{average length} = 235 \text{ ft (71.6 m)}$$

Total shortening strain

$$S = 38 + 408 + 46 = 492 \text{ micro-strain}$$

$$\text{Shortening, } a = 492 \times 10^{-6} \times 235 \times 12 = 1.38 \text{ in ( 35 mm)}$$

## Q.5 REPAIR OF RESTRAINT CRACKS

### Q.5.1 Crack Evaluation

The first step in addressing a restraint crack is to ensure that the crack has not compromised the floor's safety against overload, that is to say - the factor of safety at the strength limit state. Unlike conventionally reinforced concrete where the multitude of narrow and short cracks lead to an increase in deflection, the restraint cracks in post-tensioned floors typically do not cause a noticeable increase in the floor's deflection. If a floor's observed deflection is 15 to 20% more than the anticipated value for a similar panel without cracking, the crack's impact on the floor's structural safety should be evaluated before deciding on a repair scheme.

The next issue to review is whether the slab surfaces on either side of the crack are on the same plane. An offset between the two sides of a crack should be viewed as a sign of possible structural damage and should be investigated before repair. There is no clear rule regarding how much offset between the planes of the two sides can be tolerated. Opinions seem to favor a value not exceeding  $1/16 - 3/32$  in. (2 mm), but less than the width of the crack.

#### **Q.5.2. Cracks to Repair**

Cracks need not be repaired, if (i) they are not visible, or if visible are not objectionable; (ii) they do not impair the function of the floor; and (iii) they do not expose the member to elements of corrosion. Expansion joints in building construction, or the joint shown in Fig. Q.4.2.E-1 are in effect planned cracks at locations that do not impair the function and safety of the slab.

If there is the potential of exposure to corrosive elements, cracks that are wider than 0.1 in. (2.5 mm). should be repaired. This is in line with the allowable design criterion for members reinforced with unbonded tendons, where a crack width of 3 mm (0.12 in) is allowed by design<sup>8</sup>.

#### **Q.5.3. Time of Repair**

Restraint cracks will continue to form and widen two to three years after the tendons are stressed however the rate of crack formation and widening will decrease with time. Ideally, cracks should not be repaired until a year or two after construction. This may not be practical, however, as floors often must be placed in service soon after construction.

#### **Q.5.4 . Method of Repair**

Cracks that are working (opening and closing) such as those on the exposed surfaces of buildings that are subject to temperature variations are best repaired by routing a groove along the crack and filling the groove with a flexible sealant that is able to withstand the movement. Cracks that are continuing to widen but could expose the reinforcement to corrosive elements, or are causing objectionable leakage, should likewise be filled with flexible sealant, with the understanding that the repair may have to be redone once the crack has stopped widening. Cracks that are not expected to widen further and are not subject to movement are best repaired using a low viscosity epoxy to fill the gap.

### **Q.6 REFERENCES**

Aalami, B. O. and Barth, F. G. (1988) “ *Restraint Cracks and Their Mitigation in Unbonded Post-Tensioned Building Structures,*” Post-Tensioning Institute, Phoenix, AZ, 49 pp.

### **Q.7 NOTATIONS**

$A$  = cross sectional area of concrete associated with tributary of prestressing force  $P$ , in<sup>2</sup>, mm<sup>2</sup>;

$a$  = total shortening of a member, in, mm;

$CR$  = contribution of creep strain to shortening (Non-Dimensional ND);

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<sup>8</sup> EC2 bijan book

- $CR_0$  = base creep coefficient, ND;
- $CR_C$  = creep coefficient, ND;
- $d$  = change in length of a member;
- $E_c$  = modulus of elasticity of concrete on day 28, psi, MPa;
- $E_{ci}$  = modulus of elasticity of concrete on day of stressing, psi, MPa;
- $ES$  = total strain due to average elastic shortening;
- $f'_c$  = 28 day concrete cylinder strength, psi, MPa;
- $f'_{ci}$  = concrete cylinder strength on day of stressing, day t, psi, MPa;
- $f_{cm}(t)$  = mean concrete compressive strength at an age of t days;
- $k_c$  = volume to surface correction factor for  $CR_0$ , ND;
- $k_{cRH}$  = correction factor for  $CR_0$  for ambient relative humidity, ND;
- $k_f$  = correction factor for  $CR_0$  for concrete strength, ND;
- $k(PT)$  = correction factor for  $CR_0$  for the average precompression from post-tensioning, ND;
- $k_{v/s}$  = correction factor for base shrinkage for volume to surface ration (V/S), ND;
- $L$  = total length of a member, ft, m;
- $P$  = prestressing force; lb, kN;
- $S$  = exposed surface area of a typical unit length of concrete member, in<sup>2</sup>, mm<sup>2</sup>;
- $SH$  = contribution of shrinkage strain to shortening (Non-Dimensional ND);
- $s$  = a coefficient which depends on the type of cement, ND;
- $t$  = age of concrete in days;
- $T$  = change in temperature, C<sup>0</sup>, F<sup>0</sup>;
- $V$  = concrete volume of a typical unit length of concrete member, in<sup>3</sup>, mm<sup>3</sup>;
- $W$  = unit weight of concrete, pcf, kg/m<sup>3</sup>;
- $\alpha$  = coefficient of thermal expansion. / C<sup>0</sup>, /F<sup>0</sup>;